

ADVANCED SUBSIDIARY GCE MATHEMATICS

Core Mathematics 2

QUESTION PAPER

4722

Candidates answer on the printed answer book.

OCR supplied materials:

- Printed answer book 4722
- List of Formulae (MF1)

Other materials required:

• Scientific or graphical calculator

Friday 20 May 2011 Afternoon

Duration: 1 hour 30 minutes

INSTRUCTIONS TO CANDIDATES

These instructions are the same on the printed answer book and the question paper.

- The question paper will be found in the centre of the printed answer book.
- Write your name, centre number and candidate number in the spaces provided on the printed answer book. Please write clearly and in capital letters.
- Write your answer to each question in the space provided in the printed answer book. Additional paper may be used if necessary but you must clearly show your candidate number, centre number and question number(s).
- Use black ink. Pencil may be used for graphs and diagrams only.
- Read each question carefully. Make sure you know what you have to do before starting your answer.
- Answer **all** the questions.
- Do **not** write in the bar codes.
- You are permitted to use a scientific or graphical calculator in this paper.
- Give non-exact numerical answers correct to 3 significant figures unless a different degree of accuracy is specified in the question or is clearly appropriate.

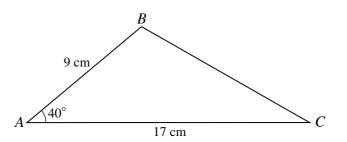
INFORMATION FOR CANDIDATES

This information is the same on the printed answer book and the question paper.

- The number of marks is given in brackets [] at the end of each question or part question on the question paper.
- You are reminded of the need for clear presentation in your answers.
- The total number of marks for this paper is **72**.
- The printed answer book consists of **12** pages. The question paper consists of **4** pages. Any blank pages are indicated.

INSTRUCTION TO EXAMS OFFICER / INVIGILATOR

• Do not send this question paper for marking; it should be retained in the centre or destroyed.



The diagram shows triangle ABC, with AB = 9 cm, AC = 17 cm and angle $BAC = 40^{\circ}$.

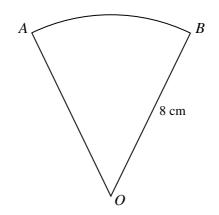
- (i) Find the length of *BC*. [2]
- (ii) Find the area of triangle *ABC*. [2]
- (iii) D is the point on AC such that angle $BDA = 63^{\circ}$. Find the length of BD. [3]

2 (i) Find
$$\int (6x^{\frac{1}{2}} - 1) dx$$
. [3]

(ii) Hence find the equation of the curve for which $\frac{dy}{dx} = 6x^{\frac{1}{2}} - 1$ and which passes through the point (4, 17). [3]



1

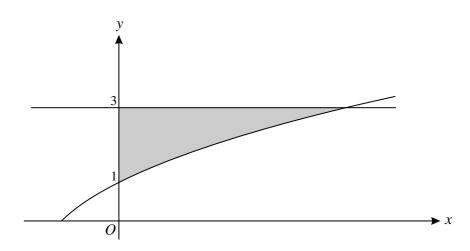


The diagram shows a sector AOB of a circle, centre O and radius 8 cm. The perimeter of the sector is 23.2 cm.

[3]

[2]

(ii) Find the area of the sector.



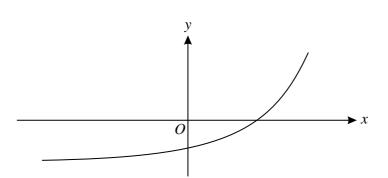
The diagram shows the curve $y = -1 + \sqrt{x+4}$ and the line y = 3.

(i) Show that
$$y = -1 + \sqrt{x+4}$$
 can be rearranged as $x = y^2 + 2y - 3$. [2]

- (ii) Hence find by integration the exact area of the shaded region enclosed between the curve, the y-axis and the line y = 3. [5]
- 5 The first four terms in the binomial expansion of $(3 + kx)^5$, in ascending powers of x, can be written as $a + bx + cx^2 + dx^3$.
 - (i) State the value of *a*. [1]
 - (ii) Given that b = c, find the value of k. [5]
 - (iii) Hence find the value of d.
- 6 The cubic polynomial f(x) is defined by $f(x) = x^3 + x^2 11x + 10$.
 - (i) Use the factor theorem to find a factor of f(x). [2]
 - (ii) Hence solve the equation f(x) = 0, giving each root in an exact form. [6]
- 7 (a) The first term of a geometric progression is 7 and the common ratio is -2.
 - (i) Find the ninth term. [2](ii) Find the sum of the first 15 terms. [2]
 - (b) The first term of an arithmetic progression is 7 and the common difference is -2. The sum of the first *N* terms is -2900. Find the value of *N*. [5]

[Questions 8 and 9 are printed overleaf.]

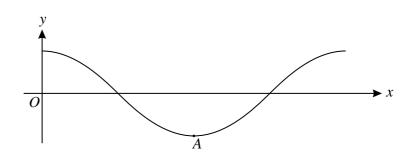
[2]



The diagram shows the curve $y = 2^x - 3$.

- (i) Describe the geometrical transformation that transforms the curve $y = 2^x$ to the curve $y = 2^x 3$. [2]
- (ii) State the y-coordinate of the point where the curve $y = 2^x 3$ crosses the y-axis. [1]
- (iii) Find the *x*-coordinate of the point where the curve $y = 2^x 3$ crosses the *x*-axis, giving your answer in the form $\log_a b$. [2]
- (iv) The curve $y = 2^x 3$ passes through the point (p, 62). Use logarithms to find the value of p, correct to 3 significant figures. [3]
- (v) Use the trapezium rule, with 2 strips each of width 0.5, to find an estimate for $\int_{3}^{4} (2^{x} 3) dx$. Give your answer correct to 3 significant figures. [3]

9 (a)



The diagram shows part of the curve $y = \cos 2x$, where x is in radians. The point A is the minimum point of this part of the curve.

- (ii) State the coordinates of *A*. [2]
- (iii) Solve the inequality $\cos 2x \le 0.5$ for $0 \le x \le \pi$, giving your answers exactly. [4]
- (b) Solve the equation $\cos 2x = \sqrt{3} \sin 2x$ for $0 \le x \le \pi$, giving your answers exactly. [4]



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1 (i)	$BC^{2} = 9^{2} + 17^{2} - 2 \ge 9 \ge 17 \ge \cos 40^{\circ}$ BC = 11.6 cm	M1		Attempt use of correct cosine rule	Must be correct formula seen or implied, but allow a slip when evaluating eg omission of 2, or incorrect use of an additional big bracket. Allow M1 even if subsequently evaluated in radian mode (23.96). Allow M1 if expression is not square rooted, as long as it is clear that correct formula was used ie either $BC^2 = \dots$ or even just $a^2 =$ \dots if the power disappears from <i>BC</i> .
		A1	2	Obtain 11.6, or better	Actual answer is 11.644329 so allow more accurate answer as long as it rounds to 11.64
(ii)	$area = \frac{1}{2} \times 9 \times 17 \times \sin 40$ $= 49.2 \text{ cm}^2$	M1		Attempt triangle area using (½) <i>ab</i> sin <i>C</i> , or equiv	Condone omission of $\frac{1}{2}$ from this formula, but no other errors allowed. If using right-angled triangle, must use $\frac{1}{2}bh$ with reasonable attempt at perpendicular sides. Allow M1 if subsequently evaluated in radian mode (57.00). If using 40°, must be using sides of 9 and 17, not 11.6 from (i). If using another angle, can still get M1 as long as sides used are consistent with this angle.
		A1	2	Obtain 49.2, or better	Actual answer is 49.17325 so allow more accurate answer as long as it rounds to 49.17 Must come from correct working only.
(iii)	$\frac{BD}{\sin 40} = \frac{9}{\sin 63}$ $BD = 6.49 \text{ cm}$	M1		Attempt use of correct sine rule, or equiv, to find length <i>BD</i>	No further rearrangement required. Could have both fractions the other way up. Must be angles of 40° and 63° if finding <i>BD</i> directly. Must be attempting <i>BD</i> , so using 77° to find <i>AD</i> is M0 unless attempt is then made to find <i>BD</i> by any valid method. Placing <i>D</i> on <i>BC</i> is M0.
		A1		Obtain correct unsimplified expression involving <i>BD</i> as the only unknown	Can still get A1 even if evaluated in radians (40.07). If using a multi-step method (eg use 77^{0} to find <i>AD</i> and then use cosine rule to find <i>BD</i>) then this A mark is only given when a correct (unsimplified) expression involving <i>BD</i> as the only unknown is obtained.
		A1	3 7	Obtain 6.49, or better	Actual answer is 6.492756 so allow more accurate answer as long as it rounds to 6.493 Must come from correct working only not eg sin 117.

2 (i)	$\int \left(6x^{\frac{1}{2}} - 1 \right) dx = 4x^{\frac{3}{2}} - x + c$	M1	Obtain $kx^{\frac{3}{2}}$	Any <i>k</i> , as long as numerical. Allow both M1 and A1 for equiv eg $x\sqrt{x}$
		A1	Obtain $4x^{\frac{3}{2}}$	Allow for unsimplified coefficient as well (ie $^{6}/_{1.5}$).
		B1 3	Obtain $-x$ (don't penalise lack of $+c$)	Allow -1 <i>x</i> .
				Maximum of 2 marks if \int or dx still present in final answer. Maximum of 2 marks if not given as one expression – eg the two terms are integrated separately and never combined.
(ii)	$y = 4x^{\frac{3}{2}} - x + c$ 17 = 32 - 4 + c \Rightarrow c = -11 hence $y = 4x^{\frac{3}{2}} - x - 11$	M1*	State or imply $y =$ their integral from (i)	Must have come from integration attempt ie increase in power by 1 for at least one term, but allow if -1 disappeared in part (i) ie at least one of the M1 and the B1 must have been awarded in part (i). Can still get this M1 if no + c. The y does not have to be explicit – it could be implied by eg 17 = F(4). M0 if they start with y = their integral from (i), but then attempt to use $y - 17 = m(x - 4)$. This is a re-start and gains no credit.
		M1d*	Attempt to find c using (4, 17)	M0 if no + c . M0 if using $x = 17$, $y = 4$.
		A1 3	Obtain $y = 4x^{\frac{3}{2}} - x - 11$	Coefficients now need to be simplified, so $-1x$ is A0. Allow A1 for equiv eg $x\sqrt{x}$ Must be an equation ie $y =$, so A0 for 'equation =' or 'f(x) ='
		6		

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3 (i)	perimeter = $2r + r\theta$ 16 + 8θ = 23.2 8θ = 7.2	B1*	State or imply that arc length 8θ , or equiv in degrees ie $\theta'_{360} \ge 16\pi$	Allow B1 by implication for $^{23.2}/_{8}$ or equivalent in degrees.
	$\theta = 0.9$ rads	M1d*	Equate attempt at perimeter to 23.2 and attempt to solve for θ	Need to get as far as attempting θ . Must include 2 radii and correct expression for arc length, either in radians or degrees. M0 if using chord length.
		A1 3	Obtain $\theta = 0.9$ rads	Obtaining 0.9 and then giving final answer as 0.9π is A0 – do not isw as this shows lack of understanding. Finding θ in degrees (51.6°) and then converting to radians can get A1 as long as final answer is 0.9 (and not eg 0.9006 from premature approximation).
(ii)	$\frac{1}{2} \ge 8^2 \ge 0.9 = 28.8$	M1	Attempt area of sector using $(\frac{1}{2}) r^2 \theta$	Condone omission of $\frac{1}{2}$, but no other error. Allow if incorrect angle from part (i), as long as clearly intended to be in radians. Allow equivalent method using fractions of the area. Allow working in degrees as long as it is a valid method. Allow M1 if using 0.9π (even if 0.9 was answer to (i)), as long as clearly attempting ($\frac{1}{2}$) $r^2\theta$ with error on angle rather then ($\frac{1}{2}$) $\pi r^2\theta$.
		A1 2		Or any exact equiv. If 0.9 obtained incorrectly in part (i), full credit can still be gained in part (ii). Condone minor inaccuracies from working in degrees, as long as final answer is given as 28.8 exactly.

4 (i) x x x	$x + 4 = (y + 1)^{2}$ x + 4 = y ² + 2y + 1 x = y ² + 2y - 3 A.G.			Attempt to make <i>x</i> the subject	Allow M1 for $x = (y \pm 1)^2 \pm 4$ only. Allow M1 if $(y + 1)^2$ becomes $y^2 + 1$, but only if clearly attempting to square the entire bracket – squaring term by term is M0. Must be from correct algebra, so M0 if eg $\sqrt{(x + 4)} = \sqrt{x} + \sqrt{4}$ is used.
		A1	2	Verify $x = y^2 + 2y - 3$	Need to see an extra step from $(y + 1)^2 - 4$ to given answer ie explicit expansion of bracket. No errors seen.
					SR B1 for verification, using $y = -1 + \sqrt{(y^2 + 2y - 3 + 4)}$, and confirming relationship convincingly, or for rearranging $x = f(y)$ to obtain given $y = f(x)$.
(ii)	$\int_{1}^{3} (y^{2} + 2y - 3) dy = \left[\frac{1}{3}y^{3} + y^{2} - 3y\right]_{1}^{3}$ $= (9 + 9 - 9) - (\frac{1}{3} + 1 - 3)$	B1		State or imply that the required area is given by $\int_{1}^{3} (y^{2} + 2y - 3) dy$	No further work required beyond stating this. Allow if $3x$ appears in integral. Any further consideration of other areas is B0.
	$= (9) - (-1^{2}/_{3})$ $= 10^{2}/_{3}$	M1		Attempt integration	Increase in power of y by 1 for at least two of the three terms. Can still get M1 if the -3 disappears, or becomes $3x$. Allow M1 for integrating a function of y that is no longer the given one, eg subtracted from 3, or using their incorrect rearrangement from part (i).
		A1ft		Obtain at least two correct terms	Allow for unsimplified coefficients. Allow follow-through on any function of y as long as at least 2 terms and related to the area required. Condone \int , dy or + c present.
		M1		Attempt $F(3) - F(1)$ for their integral	Must be correct order and subtraction. This is independent of first M1 so can be given for substituting into any expression other than $y^2 + 2y - 3$, including $2y + 2$. If last term is $3x$ allow M1 for using 3 and 1 throughout integral, but M0 if x value is used instead.
		A1	5 7	Obtain 10 ² / ₃ aef	Must be an exact equiv so 10.6 is fine (but $9^{5}/_{3}$ is A0). 10.7, 10.66 or $10^{2}/_{3} + c$ are A0. Must come from correct integral, so A0 if from $3x$. Must be given as final answer, so further work eg subtracting another area is A0 rather than ISW.
					Answer only is $0/5$, as no evidence is provided of integration. SR Finding the shaded area by direct integration with respect to x (ie a C3 technique) can have 5 if done correctly, 4 if non-exact decimal given as final answer but no other partial credit.

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(i)	243	B1	1	State 243, or 3 ⁵	B0 if other terms still present eg ${}^{5}C_{0}$ or 3^{0} . Could be part of a longer expansion, in which case ignore all other terms unless also solely numerical.
(ii)	$2^{nd} \text{ term} = 5 \text{ x } 3^4 \text{ x } (kx) = 405kx$ $3^{rd} \text{ term} = 10 \text{ x } 3^3 \text{ x } (kx)^2 = 270k^2x^2$ $405k = 270k^2 \Longrightarrow k = 1.5$	B1		Obtain 405 <i>k</i> as coeff of <i>x</i>	Either stated, or written as $405kx$. Allow unsimplified expression ie 5 x 3 ⁴ x k or 5 x 3 ⁴ x (kx), even is subsequently incorrectly evaluated. B0 if still ⁵ C ₁ unless later clearly used as 5.
		M1		Attempt coeff of x^2	Needs to be an attempt at a product involving the relevant binomial coefficient (not just ${}^{5}C_{2}$ unless later seen as 10), 3 ³ and an intention to square the final term (but allow for kx^{2}). 67.5 k^{2} is M0 (from ${}^{5}/{}_{2} \ge 3^{3}$).
		A1		Obtain 270 <i>k</i> ²	Allow unsimplified ie $10 \ge 3^3 \ge k^2$ or $10 \ge 3^3 \ge (kx)^2$ even if subsequently incorrectly evaluated. Allow $270k^2$ following $10 \ge 3^3 \ge kx^2$ ie an invisible bracket was used.
		M1		Equate coefficients and attempt to solve for <i>k</i>	Must be one linear and one quadratic term in k , and must be appropriate method to solve this two term quadratic eg factorise o cancel common factor of k . Condone powers of x still present when equated, as long as not actually used in solution method. Could still gain M1 if incorrect, or no, binomial coefficients used – each term must be product of powers of 3 (poss incorrect), correct powers of k and any binomial coefficient used.
		A1	5	Obtain $k = 1.5$ (ignore any mention of $k = 0$)	Any exact equivalent, including unsimplified fraction. Could be implied by writing $(3 + 1.5x)^5$.
					NB If expansion is given as $405kx + 270kx^2$, and candidate then concludes that $k = \frac{405}{270}$ this is B1 M1 only as k^2 never seen.

(iii) $10 \ge 3^2 \ge 1.5^3 = 303.75$	M1	Attempt 10 x 3 ² x <i>k</i> ³	Need to see 10 so just ${}^{5}C_{3}$ is not good enough for M1. Need to see correct powers intended, even if incorrectly evaluated. This includes a clear intention to cube 1.5 (or their <i>k</i>), so 10 x 9 x $1.5x^{3} = 135x^{3}$ is M0. Can get M1 if using their incorrect <i>k</i> , including 0, but M0 if the value of <i>k</i> used is different to that obtained in (ii). For incorrect numerical answer (following incorrect <i>k</i>), we need to see evidence of method – it cannot be implied by answer only. If k = -1, 0 or 1 we still need to see evidence of cubing. If 90 k^{3} is seen in part (ii) (or even (i)) then this is sufficient for M1 unless contradicted by their work in part (iii). Allow if still <i>k</i> rather than numerical.
	A1	2 Obtain 303.75 (allow $303.75x^3$)	Or any exact equivalent. Ignore if subsequently rounded eg to 304 as long as exact value seen.
		8	If 1.5 obtained incorrectly in part (ii), full credit can still be gained in part (iii).

6(i)	f(1) = 1 $f(-1) = 21f(2) = 0$, hence $(x - 2)$ is a factor	M1		Attempt use of factor theorem at least once	Just substituting at least one value for x is enough for M1, showing either the working or the result, or both. Just stating $f(a) = k$ is enough – don't need to see term by term evaluation. If result is inconsistent with the $f(a)$ being attempted, then we do need to see evidence of method used. No conclusion required. M0 A0 for division attempts, even if considering remainder.
		A1	2	Obtain factor of $(x - 2)$	Allow A1 for sight of $(x - 2)$, even if $x = 2$ also present. No words required, but penalise if used incorrectly ie A0 if explicitly labelled as 'root'. A0 if $(x - 2)$ not seen in this part, even if subsequently used in (ii). SR B1 for $(x - 2)$ stated with no justification, and no incorrect terminology.
(ii)	$f(x) = (x - 2)(x^{2} + 3x - 5)$ $x = \frac{-3 \pm \sqrt{29}}{2} \text{ or } x = 2$	M1		Attempt complete division by a linear factor, or equivalent ie inspection or coefficient matching	Need linear factor of form $(x \pm a)$, $a \neq 0$. Allow if factor different to their answer to (i), inc no answer to (i). Must be complete attempt at all three terms. If long division then need to be subtracting lower line; if coefficient matching then need to be considering all possible terms from their expansion to equate to relevant coefficient from cubic; if inspection then expansion must give at least one correct coefficient for the two middle terms in the cubic.
		A1		Obtain $x^2 + 3x + c$ or $x^2 + bx - 5$	Obtain x^2 and one other correct term. Just having two correct terms does not imply M1 – need to look at method used for third term. If coefficient matching allow for stating values eg $a = 1$ etc. If quadratic factor given with minimal working in (ii), there may be more evidence of method shown in (i).
		A1		Obtain $x^2 + 3x - 5$	Could appear as quotient in long division, or as part of product if inspection. If coefficient matching, must now be explicitly stated rather than just $a = 1$, $b = 3$, $c = -5$.
		M1		Attempt to solve quadratic equation	Using quadratic formula or completing the square – see extra guidance sheet. Quadratic must come from division attempt, even if this was not good enough for first M1.
		A1		Obtain $\frac{1}{2}(-3 \pm \sqrt{29})$	Or $^{-3}/_2 \pm \sqrt{29}/_4$ from completing the square. Ignore terminology and ignore if subsequently given as factors, as long as seen fully simplified as roots.
		B1	6 8	State 2 as root, at any point	Must be stated in this part, not just in part (i). Ignore terminology.

7(a) (i)	$u_9 = 7 \ge (-2)^8$ = 1792	M1		Attempt u_9 using ar^8	Allow for 7 x -2^8 . Using $r = 2$ will be marked as a misread.
		A1	2	Obtain 1792	Condone brackets not being shown explicitly in working.
					SR B2 for listing terms, as long as signs change. Need to stop at u_9 or draw attention to it in a longer list.
(ii)	$S_{15} = \frac{7(1-(-2)^{15})}{1-(-2)}$ = 76,461	M1		Attempt sum of GP using correct formula	Must be using correct formula, so denominator of 1–2 is M0 unless $1 - r$ clearly seen previously. If $n = 14$ used, then only mark as misread if no contradictory evidence seen – starting with $S_{15} =$ implies error in using in formula so M0.
		A1	2	Obtain 76,461	Condone brackets not being shown explicitly in working.
					SR B2 for listing terms and then manually adding them.
(b)	$\frac{N}{2} (2 \times 7 + (N-1) \times -2) = -2900$ $\frac{N(16 - 2N)}{2} = -5800$ $\frac{N^2 - 8N - 2900}{10} = 0$ $\frac{N - 58}{N} + 50 = 0$	B1		State correct unsimplified S_N	If $(n-1)d$ is written as $(N-1)-2$, then give benefit of doubt and allow B1, even if misused in subsequent work (eg becomes $N-3$), unless there is clearly an error in the formula used.
	(N - 38)(N + 30) = 0 N = 58	M1		Equate attempt at S_N to -2900 and rearrange to $f(N) = 0$	Must be attempt at S_N for an AP, so using u_N or GP formulae will be M0. M0 if $(N-1) - 2$ becomes $N-3$. To give M1 at least one of the two terms in the bracket must have been multiplied by -2. Can still get M1 if incorrect formula as long as recognisable, and is quadratic in N . Expand brackets and collect all terms on one side of equation. Allow slips eg not dividing all terms in bracket by 2.
		A1		Obtain $N^2 - 8N - 2900 = 0$	Any equivalent form as long as $f(N) = 0$ (but condone 0 not being explicit).
		M1		Attempt to solve 3 term quadratic	Any valid method – as long as it has come from equating an attempt at S_N of an AP to -2900
		A1	5	Obtain 58 only	58 must clearly be intended as only final answer – could be through underlining, circling or deleting other value for N . No need to see other value for N – if seen, allow slips as long as factorisation / substitution into formula is correct.
			9		58 from answer only or trial and improvement can get 5/5. 58 and -50 with no working is 4/5.

8 (i)	translation of 3 units in negative y-direction	B 1		State translation	Not shift, move etc.
		B1	2	State or imply 3 units in negative <i>y</i> -direction	Independent of first B1. Statement needs to clearly intend a vertical downwards move of 3, without ambiguity or contradiction, such as '3 down', '-3 in the <i>y</i> direction' etc or vector notation. B0 if direction unclear, such as 'in the <i>y</i> -axis' (could be along or towards) or 'along the <i>y</i> -axis' (unless direction made clear). Allow '3' or '3 units' but not '3 places', '3 spaces', '3 squares', '3 coordinates' or mention of (scale) factor of 3. If both a valid statement and an ambiguous statement are made eg '3 units down on the <i>y</i> -axis' then still award B1. Ignore irrelevant statements, such as where the <i>y</i> -intercept is, whether correct or incorrect. Give BOD on double negatives eg 'down the <i>y</i> -axis by – 3 units' unless clearly wrong or contradictory eg 'negative <i>y</i> -direction by $\binom{-3}{0}$ '.
(ii)	<i>y</i> = -2	B1	1	State or imply $y = -2$	Just stating -2 is enough. B0 for final answer of $2^0 - 3$ or $1 - 3$. (-2, 0) is B0 unless -2 already seen or implied as <i>y</i> -coordinate.
(iii)	$2^{x} = 3$ $x = \log_{2} 3$	M1		Attempt to solve $2^x - 3 = 0$	Rearrange to $2^x = 3$, introduce logarithms (could be no base or any base as long as consistent) and then attempt expression for <i>x</i> . M0 for $x = \log_3 2$. M1 A0 for alternative, correct, log expressions such as \log_3/\log_2 or $1/\log_3 2$. Decimal equivalent of 1.58 can get M1 A0. $x = \log_2 (y + 3)$ is M0 (unless <i>y</i> then becomes 0).
		A1	2	State log ₂ 3	Doesn't need to be $x =$ Change of base is not on the specification, but is a valid method and can gain both marks. Allow if base not initially specified, but then both logs become base 2. NB $x - \log_2 3 = 0$ leading to correct answer, can get full marks as there is no incorrect statement seen.

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(iv)	$2^{p} = 65$ log $2^{p} = \log 65$ plog $2 = \log 65$	M1*		Rearrange equation and introduce logs (or log ₂)	Must first rearrange to $2^p = k$, with k from attempt at 62 ± 3 , before introducing logs. Can use logs to any base, as long as consistent, or equiv with log ₂ .
	<i>p</i> = 6.02	M1d*		Drop power and attempt to solve	Dependent on first M1. $p = \log_2 k$ will gain both M marks in one step. If taking logs to any other base, or no base, or \log_2 on both sides then need to drop power of p and attempt to solve using a sound algebraic method ie $p = \frac{\log k}{\log 2}$.
		A1	3	Obtain 6.02, or better	Decimal answer reqd, if more than 3sf it must be in range [6.022, 6.023].
					Answer only, or trial and improvement, is 0/3 as no evidence of using logs as requested.
(v)	$0.5 \times 0.5 \times \{2^{3} - 3 + 2(2^{3.5} - 3) + 2^{4} - 3\}$ = 8.66	M1		Attempt <i>y</i> -values at $x = 3, 3.5, 4$	M0 if other <i>y</i> -values also found (unless not used in trap rule). Allow M1 for using incorrect function as long as still clearly <i>y</i> -values that are intended to be the original function eg $2x - 3$ or $2^{(x-3)}$.
		M1		Attempt correct trapezium rule	Must be correct structure ie $0.5 \ge 0.5 \ge (y_0 + 2y_1 + y_2)$. Must be finding area from 3 to 4, so using eg $x = 0$, 0.5, 1 is M0. Allow if still in terms of y_0 etc as long as these have been clearly defined elsewhere. Using <i>x</i> -values in trapezium rule is M0, even if labelled <i>y</i> -values. Allow a different number of strips (except 1) as long as their <i>h</i> is consistent with this, and the limits are still 3 and 4.
		A1	3	Obtain 8.66, or better	If final answer given to more than 3sf, allow answers in range [8.655, 8.657].
			11		Exact answer from integrating $e^{x \ln 2} - 3$ is 0/3. Answer only is 0/3. Attempting integration before using trapezium rule is 0/3. Using two separate trapezia is fine.

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9(a) (i)	π radians	B1	1	State π	Allow 3.14 radians or 180° . B0 for $0 \le x \le \pi$.
(ii)	$(\pi/2, -1)$	B1		State $x = \pi/2$	Allow 1.57 radians, or better. Allow $A = \pi/2$. B0 for 90 ⁰ .
		B1	2	State $y = -1$	Allow $\cos 2A = -1$.
					SR Award B1 for $(-1, \pi/2)$
(iii)	$\frac{\cos 2x = 0.5}{2x = \frac{\pi}{3}, \frac{5\pi}{3}}$	M1		Attempt correct solution method	Inverse cos and then divide by 2, to find at least one angle.
	$2x - \frac{7}{3}, \frac{7}{3}$ x = $\frac{\pi}{6}, \frac{5\pi}{6}$ hence $\frac{\pi}{6} \le x \le \frac{5\pi}{6}$	A1		Obtain $\pi/_6$ (allow 0.524 or 30°)	Just mark angle, ignore any (in)equality signs.
	$\frac{1}{6} \leq x \leq \frac{1}{6}$	A1		Obtain $\frac{5\pi}{6}$ (allow 2.62 or 150°)	Needs to be single term so $\pi - \pi/6$ is A0. Just mark angle, ignore any (in)equality signs. A0 if any other angles in range $0 \le x \le \pi$.
		A1	4	Obtain $\pi/6 \le x \le 5\pi/6$ (exact radians only)	Allow two separate inequalities as long as both correct and linked by 'and' (not 'or', a comma or no link). Mark final answer and condone incorrect inequality signs elsewhere in solution.
					 SR If alternative methods (eg double angle formulae) or inspection are used (or no method shown at all) then mark as B2 Obtain one correct angle (degrees or radians) A1 Obtain second correct angle – and no others A1 Obtain correct inequality (exact radians only)

(b)	$\tan 2x = \frac{1}{\sqrt{3}}$ $2x = \frac{\pi}{6}, \frac{7\pi}{6}$ $x = \frac{\pi}{12}, \frac{7\pi}{12}$	B 1		Obtain $\tan 2x = 1/\sqrt{3}$	Allow for decimal equiv ie $\tan 2x = 0.577$ Allow for $\sqrt{3} \tan 2x = 1$.
	$x = 7_{12}, 7_{12}$	M1		Attempt correct solution method of $\tan 2x = k$	Inverse tan and then divide by 2, to find at least one angle. Could follow error eg tan $2x = \sqrt{3}$, even if tan $2x = \frac{\cos 2x}{\sin 2x}$ clearly used.
		A1		Obtain one correct angle	Could be exact $(\pi/_{12} \text{ or }^{7\pi}/_{12})$, decimals (0.262 or 1.83) or degrees (15° or 105°). Must come from correct working only.
		A1	4	Obtain both correct angles	Must now both be in exact radians. A0 if any other angles in range $0 \le x \le \pi$.
			11		
	OR $\cos^2 2x = 3\sin^2 2x$ $4\sin^2 2x = 1$ $4\cos^2 2x = 3$ $4\cos^2 2x = 3$	B1		Obtain correct equation in either $\sin^2 2x$ or $\cos^2 2x$	Square both sides and use $\sin^2 2x + \cos^2 2x = 1$ to obtain $4\sin^2 2x = 1$ or $4\cos^2 2x = 3$, or any equiv, including unsimplified eg $1 - \sin^2 2x = 3\sin^2 2x$.
	$\sin 2x = \pm \frac{1}{2} \cos 2x = \pm \frac{\sqrt{3}}{2} \cos 2x = \pm \frac{\sqrt{3}}{2} \cos 2x = \frac{1}{2} \cos 2x = \frac{1}{2} \sin 2x = $	M1		Attempt correct solution of $\sin 2x = k$ or $\cos 2x = k$	Inverse sin or cos and then divide by 2, to find at least one angle.
	$x = \pi/12, \pi/12$	A1		Obtain one correct angle	Could be exact $(\pi/_{12} \text{ or } 7\pi/_{12})$, decimals (0.262 or 1.83) or degrees (15° or 105°). Must come from correct working only.
		A1		Obtain both correct angles	Must now both be in exact radians. A0 if any other angles in range $0 \le x \le \pi$.
					 SR If using alternative methods, such as more advanced trig identities, or no method at all shown, then mark as B3 Obtain one correct angle, (degrees or radians)with no errors seen B1 Obtain second correct angle, now both in radians